

Abstract: In this talk, we consider the following Cauchy problem for  $1 < \alpha \leq 2$

$$(1) \quad -i\partial_t u + (-\Delta)^{\frac{\alpha}{2}} u = \sigma(|\cdot|^{-\alpha} * |u|^2)u, \quad u(0, \cdot) = \varphi.$$

We prove that there exists a globally well-posed solution to (1) and the solution scatters to free waves asymptotically as  $t \rightarrow \pm\infty$  whenever the initial data is radial and sufficiently small in  $L^2(\mathbb{R}^3)$ . This result is shown to be optimal by proving the discontinuity of the flow map in the super-critical range. We employ the standard contraction argument in a function space constructed based on the space of bounded quadratic variation  $V^2$ . The main ingredients for the proof are  $L^2(\mathbb{R}^{1+3})$  bilinear estimates for free solutions and its transference to adapted  $V^2$  spaces. This is joint work with Sebastian Herr.